

LEZIONI

LE FORMULE DELLA GONIOMETRIA

Abbiamo qui raccolto le formule che permettono di calcolare le funzioni di un angolo conoscendo quelle di uno o più angoli legati al primo da una certa relazione

FORMULE DI ADDIZIONE E DI SOTTRAZIONE

1. $sen(\alpha \pm \beta) = sen\alpha \cos \beta \pm \cos \alpha sen\beta$
2. $cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp sen\alpha sen\beta$
3. $tg(\alpha \pm \beta) = \frac{tg\alpha \pm tg\beta}{1 \mp tg\alpha \cdot tg\beta}$ $\alpha, \beta \neq \frac{\pi}{2} + k\pi$ e $\alpha \pm \beta \neq \frac{\pi}{2} + k\pi$
4. $ctg(\alpha \pm \beta) = \frac{1 \mp tg\alpha \cdot tg\beta}{tg\alpha \pm tg\beta} = \frac{ctg\alpha \cdot ctg\beta \mp 1}{ctg\beta \pm ctg\alpha}$ $\alpha, \beta \neq k\pi$ e $\alpha \pm \beta \neq k\pi$

FORMULE DI DUPLICAZIONE

5. $sen 2\alpha = 2sen\alpha \cos \alpha$
6. $cos 2\alpha = \cos^2 \alpha - sen^2 \alpha = 1 - 2sen^2 \alpha = 2\cos^2 \alpha - 1$
7. $tg 2\alpha = \frac{2tg\alpha}{1 - tg^2 \alpha}$ $\alpha \neq \frac{\pi}{2} + k\pi$ e $\alpha \neq \frac{\pi}{4} + k\frac{\pi}{2}$
8. $ctg 2\alpha = \frac{1 - tg^2 \alpha}{2tg\alpha} = \frac{ctg^2 \alpha - 1}{2ctg\alpha}$ $\alpha \neq k\frac{\pi}{2}$

FORMULE PARAMETRICHE

9. $sen\alpha = \frac{2t}{1+t^2}$ e $cos\alpha = \frac{1-t^2}{1+t^2}$ con $t = tg \frac{\alpha}{2}$ ($\alpha \neq \pi + 2k\pi$)

FORMULE DI BISEZIONE

10. $sen \frac{\alpha}{2} = \pm \sqrt{\frac{1 - \cos \alpha}{2}}$

$$11. \cos \frac{\alpha}{2} = \pm \sqrt{\frac{1 + \cos \alpha}{2}}$$

$$12. \operatorname{tg} \frac{\alpha}{2} = \pm \sqrt{\frac{1 - \cos \alpha}{1 + \cos \alpha}} \quad \text{o} \quad \operatorname{tg} \frac{\alpha}{2} = \pm \frac{\operatorname{sen} \alpha}{1 + \cos \alpha} \quad \text{o} \quad \operatorname{tg} \frac{\alpha}{2} = \pm \frac{1 - \cos \alpha}{\operatorname{sen} \alpha} \quad \alpha \neq \pi + 2k\pi$$

$$13. \operatorname{ctg} \frac{\alpha}{2} = \pm \sqrt{\frac{1 + \cos \alpha}{1 - \cos \alpha}} \quad \alpha \neq 2k\pi$$

FORMULE DI PROSTAFERESI

$$14. \operatorname{sen} p + \operatorname{sen} q = 2 \operatorname{sen} \frac{p+q}{2} \cos \frac{p-q}{2}$$

$$15. \operatorname{sen} p - \operatorname{sen} q = 2 \cos \frac{p+q}{2} \operatorname{sen} \frac{p-q}{2}$$

$$16. \cos p + \cos q = 2 \cos \frac{p+q}{2} \cos \frac{p-q}{2}$$

$$17. \cos p - \cos q = -2 \operatorname{sen} \frac{p+q}{2} \operatorname{sen} \frac{p-q}{2}$$

$$18. \operatorname{tg} p \pm \operatorname{tg} q = \frac{\operatorname{sen}(p \pm q)}{\cos p \cos q} \quad p, q \neq \frac{\pi}{2} + k\pi$$

$$19. \operatorname{ctg} p \pm \operatorname{ctg} q = \frac{\operatorname{sen}(p \pm q)}{\operatorname{sen} p \operatorname{sen} q} \quad p, q \neq k\pi$$

FORMULE DI WERNER

$$20. \operatorname{sen} \alpha \operatorname{sen} \beta = \frac{1}{2} [\cos(\alpha - \beta) - \cos(\alpha + \beta)]$$

$$21. \cos \alpha \cos \beta = \frac{1}{2} [\cos(\alpha + \beta) + \cos(\alpha - \beta)]$$

$$22. \operatorname{sen} \alpha \cos \beta = \frac{1}{2} [\operatorname{sen}(\alpha + \beta) + \operatorname{sen}(\alpha - \beta)]$$